1st Parameterized Algorithms & Computational Experiments Challenge

Where it came from, how it went, who won, and what's next





WHERE PACE CAME FROM

Inception

- PACE was conceived in fall 2015 when many FPT researchers gathered at the Simons institute
- Born from a feeling that parameterized algorithmics should have a greater impact on practice
- Partially inspired by the success of SAT-solving competitions in neighboring communities
- Discussions with many members of the community (thanks for all your input!) led to a steering committee and two challenge tracks for 2015-2016 with program committees
 - Track A: Treewidth
 - Track B: Feedback Vertex Set

Goals

- Investigate the applicability of algorithmic ideas from parameterized algorithmics
 - provide bridge between algorithm design&analysis theory and algorithm engineering practice
 - 2. inspire new theoretical developments
 - 3. investigate the competitiveness of analytical and design frameworks developed in the communities
 - 4. produce universally accessible libraries of implementations and repositories of benchmark instances
 - 5. encourage dissemination of the findings in scientific papers

PACE organization

Steering committee:

Holger Dell

Bart M. P. Jansen

Thore Husfeldt

Petteri Kaski

Christian Komusiewicz

Frances A. Rosamond [chair]

Saarland University & Cluster of Excellence

Eindhoven University of Technology

ITU Copenhagen and Lund University

Aalto University

Friedrich-Schiller-University Jena

University of Bergen

PACE organization

Program committee track A, Treewidth:

Isolde Adler University of Leeds

Holger Dell [chair] Saarland University and Cluster of Excellence

Thore Husfeldt ITU Copenhagen and Lund University

Lukas Larisch University of Leeds

Felix Salfelder Goethe University Frankfurt

Program committee track B, Feedback Vertex Set:

Falk Hüffner Industry

Christian Komusiewicz Friedrich-Schiller-University Jena

PACE timeline in 2015-2016



- March 1st 2016: Call for contributions, benchmark instances available, website online
- June 1st 2016: Register participation
- June 22nd 2016: Prizes and travel awards announced, sponsored by Networks
- August 1st 2016: Submission deadline
- August 24th 2016: Winner announcement

pacechallenge.wordpress.com

A word from the sponsor ...

- We are offering a 2-year postdoc position in Network Algorithms at the Eindhoven University of Technology
 - Broad range: computational geometry, graph algorithms, or FPT algorithms
 - Contact Mark de Berg (<u>m.t.d.berg@tue.nl</u>) before August 31

NETWORKS is a project of
University of Amsterdam
Eindhoven University of Technology
Leiden University
Center for Mathematics and
Computer Science (CWI)



thenetworkcenter.nl

How it went and who won

TRACK A: TREEWIDTH

PACE 2016 Track A: Tree width

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Isolde Adler
Holger Dell
Thore Husfeldt
Lukas Larisch
Felix Salfelder

PACE challenges, Track A

exact tree width

Evaluation: The running time

3 submissions

heuristic tree width

Evaluation: The obtained width

7 submissions

instances

2 submissions

<u>Treewidth</u>

Given G and k, is $tw(G) \le k$?

- NP-hard, but in time n^{k+2}
 (Arnborg, Corneil & Proskurowski 1987)
- in FPT time exp(k³) n
 (Bodlaender 1996)
- factor-5 approximation in time exp(k) n
 (Bodlaender Drange Dregi Fomin Lokshtanov Pilipczuk 2013)
- open: PTAS?

Some Applications (outside of FPT)

- Register allocation in compilers (e.g., Thorup 1998)
- Preprocessing for shortest path (e.g., Chatterjee Ibsen-Jensen Pavlogiannis 2016)
- Treewidth of specific graph families (e.g., Kiyomia Okamotob Otachic 2015)
- Preprocessing for probabilistic inference (e.g., Otten Ihler Kask Dechter 2011)

Treewidth implementations pre-PACE

- Python SAGE: slow and buggy
- Outdated C++-library without documentation
- Some non-public implementations
- No standard input/output format
- Hard to compare

The submission requirements

- repository on github.com
- 2-page abstract
- DIMACS input format
- Output: tree decomposition

Benchmark instances

- 96 control flow graphs
- 79 special "named" graphs
- 56 DIMACS graph coloring instances
- 41 random instances
- 7 incidence graphs of SAT competition instance
- 2 transit networks

281 total

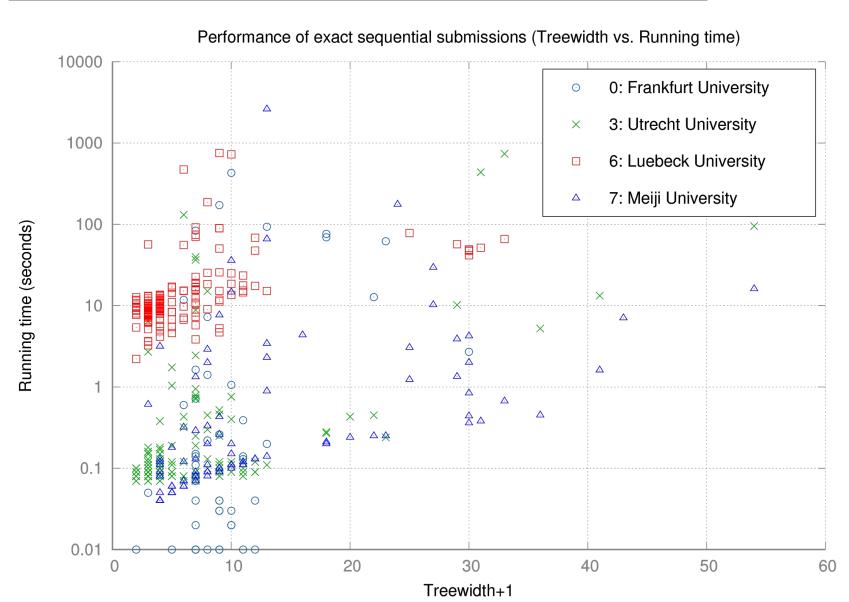
Detailed results, benchmark instances, and tools to easily reproduce the results: https://github.com/holgerdell/PACE-treewidth-testbed

Submission programming languages

- C++-11
- C# / Mono
- Java 8

Exact treewidth

Exact Treewidth Competition Results



Exact Treewidth Competition Results

instances solved in timeout:

- 166 Berndt, Bannach, Ehlers (Universtität zu Lübeck)
- 171 Larisch & Salfelder (baseline)
- 173 Bodlaender & Van der Zanden (Utrecht University)
- 199 Tamaki (Meiji University)

Algorithmic ideas

Use SAT-solver to find elimination order (Team Lübeck)

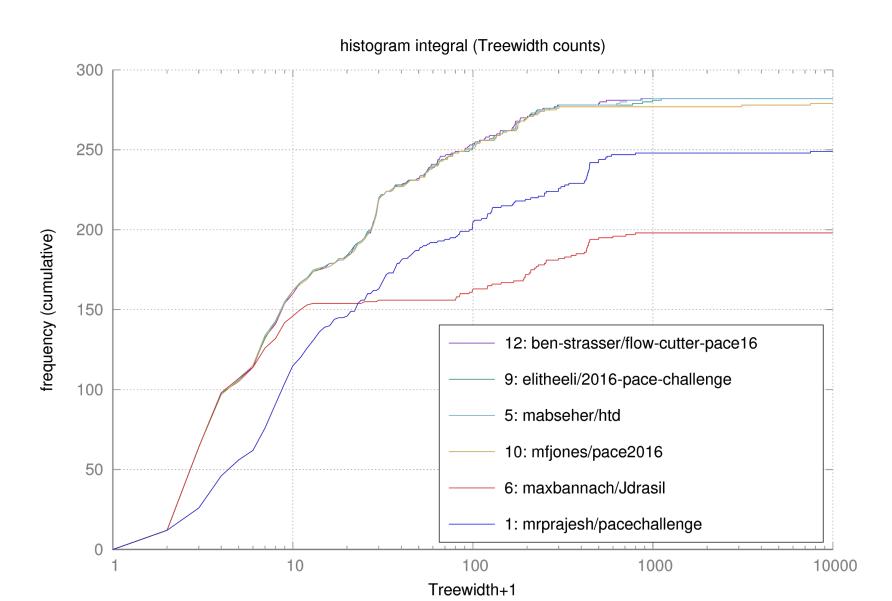
Branch on balanced separators + DP (Team Utrecht)

Tamaki:

- Modify n^k brute-force approach of Arnborg et al. (1987) in an upcoming publication
- Running time not known to be in n^{f(k)}

Heuristic treewidth

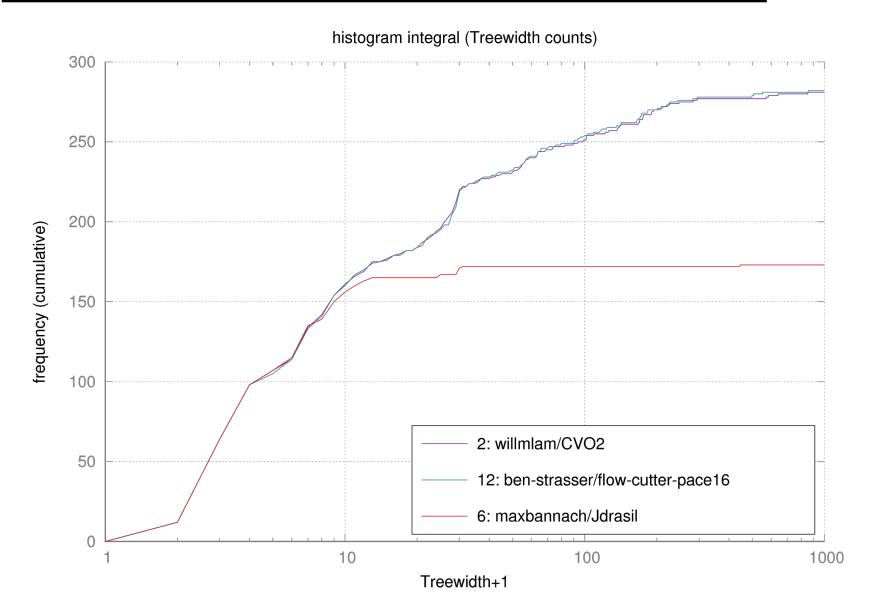
Heuristic Sequential Treewidth Competition



Heuristic Sequential Treewidth Competition



Heuristic Parallel Treewidth Competition



Evaluation Scheme

6s11-opt.gaifman.gr

submission	width after 100s
5	672
12	957
9	994
1	33279
10	33279

Preferential voting scheme

Instances=Voters

Use Schulze method to combine votes

Heuristic Competition Results

Sequential algorithm

- Ben Strasser
 (Karlsruhe Institute of Technology)
- Eli Fox-Epstein (Brown University)
- 3. Abseher, Musliu, Woltran (TU Wien)

Parallel algorithm

- Kask, Lam
 (University of California at Irvine)
- Ben Strasser(Karlsruhe Institute of Technology)
- 3. Bannach, Berndt, Ehlers (Universität zu Lübeck)

Condorcet Winners

Heuristic sequential:

12 (Strasser) better than

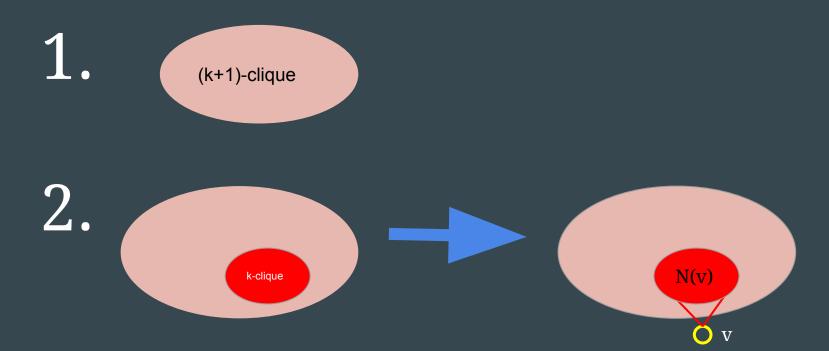
```
1 (IIT Madras) on 100% of instances
6 (Lübeck) on 95.5% of instances
10 (Australia) on 71% of instances
5 (TU Wien) on 61% of instances
9 (Fox-Epstein) on 55% of instances
```

Heuristic parallel:

2 (UC Irvine) better than

6 (Lübeck) on 99% of instances 12 (Strasser) on 63% of instances

Definition of k-Trees



subgraphs of k-trees = treewidth k graphs

elimination order: reverse of insertion order

Main Algorithmic Ideas for Heuristic TW

Minimum Fill-In Heuristic Guess elimination order:

Choose vertex v randomly so that
 few edges need to be added to turn N(v) into clique

Team Australia (rank 4)
"Turbocharging treewidth heuristics" (IPEC 2016)

PACE challenges, Track A

exact tree width

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heuristic tree width

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How it went and who won

TRACK B: FEEDBACK VERTEX SET

The 1st Parameterized Algorithms and Computational Experiments Challenge: Track B Feedback Vertex Set

Falk Hüffner Technische Universität Berlin

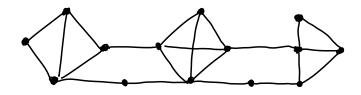
Christian Komusiewicz
Friedrich-Schiller-Universität Jena

Challenge Problem

Feedback Vertex Set

Input: An undirected graph G = (V, E).

Task: Find a minimum set $S \subseteq V$ such that G - S is a forest.

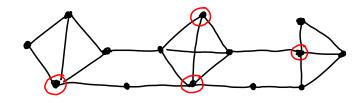


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Feedback Vertex Set is fixed-parameter tractable e.g. parameterized by solution size |S|, amenable to different techniques: branching, iterative compression, kernelization, randomized branching,...

Benchmark Instances: 230 instances, 100 public instances and 130 hidden instances

Instance origin: Social networks, biological networks, incidence graphs of CNF formulas, road networks, power networks

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	V	<i>E</i>	S
min	32	63	5
median	308.5	1305	34
Ø	2079	4185	153
max	19362	32081	6400

Winner Criterion: # solved instances within 30 minutes (each) on the set of hidden instances

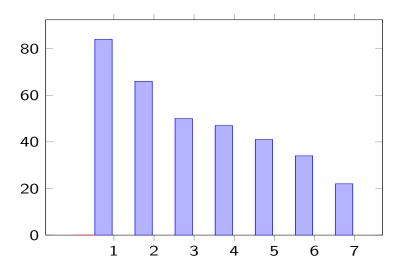
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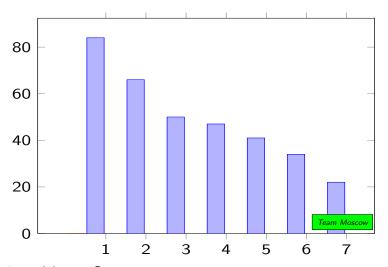
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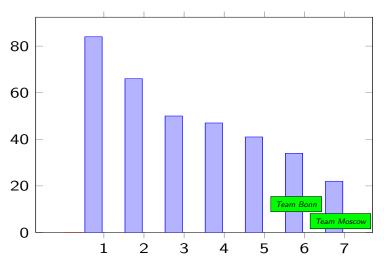
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Participation: 14 registrations, 7 submissions

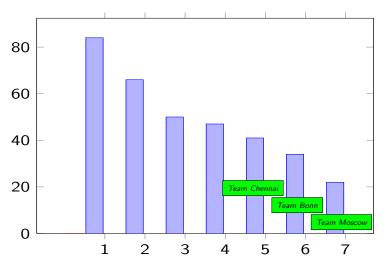




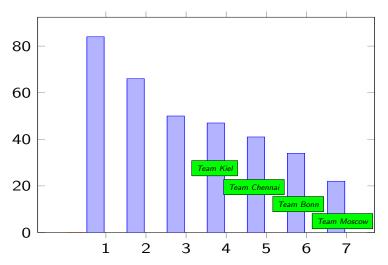
1 participant, C++ randomized branching



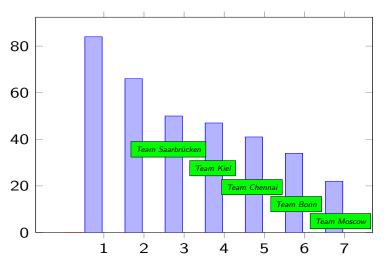
5 participants, C++ iterative compression, subcubic graphs $\in P$



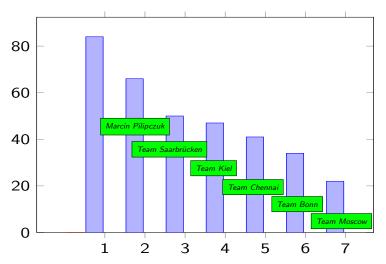
4 participants, Python branching on shortest cycle, search tree pruning via lb



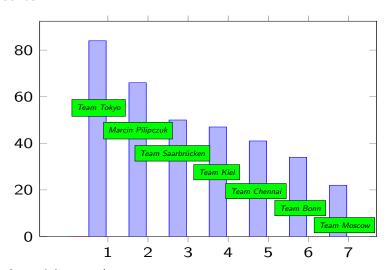
4 participants, C# iterative compression & branching, subcubic graphs $\in P$



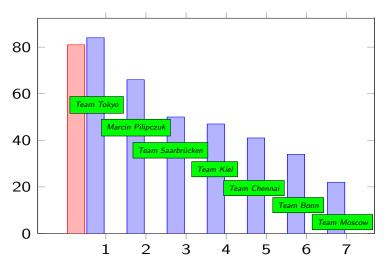
5 participants, C++, branching, search tree pruning via lower and upper bounds



1 participant, C++, branching, subcubic graphs $\in P$, DP on tree decomposition



2 participants, Java, LP-based branching and kernelization



ILP, gurobi data reduction, lazy constraints adding short remaining cycles

WHAT'S NEXT?

Long term plan

- Have a PACE challenge every year to continually drive the transition from theory to practice
 - Challenge problems may change from year to year
- PACE does not aim to be a publication venue for papers
 - Authors of submissions are encouraged to submit papers describing their implementations to established venues (IPEC, ESA track B, ALENEX, etc.)
- Desire to have the award ceremony at IPEC every year
 - (To be discussed with IPEC steering committee)

PACE 2016-2017

- PACE will again have two tracks next year
 - 1. Treewidth track
 - Similarly to this year but without a subtrack for parallel algorithms
 - 2. Track for "Problem X"
 - Problem still to be determined, to be solved exactly by FPT methods
- Time schedule:
 - 1. November 1st 2016: Announcement of problems and inputs
 - 2. March 1st 2017: Submission of prototype program to check input/output formats
 - 3. May 1st 2017: Submission of final program
 - 4. June 1st 2017: Result are announced
 - 5. Early September 2017: Award ceremony at IPEC

Input from the community

- Which "problem X" to use for the second track next year?
- Preferably, problem X:
 - Has been analyzed successfully from the theoretical perspective, with several different approaches for obtaining FPT algorithms
 - 2. Is relevant in practice and it is possible to find real-world instances with moderate parameter values



Feedback

• Comments? Suggestions? Tips?

History of parameterized complexity

Parameterized Downey & complexity Fellows book newsletter Kernelization lower NP-completeness bounds 1975 1980 1985 1990 1995 2000 2005 2010 2015 Planar Dominating SET kernel 1st PACE **Parameterized** Graph (in)tractability 1st I(W)PEC Minors Conference 1st **Wor**kshop on Theorem **Ker**nelization