# Algorithms for Model Checking (2IMF35) Lecture 12 Retrospect + Outlook

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Retrospect 2/1	7
Part I: basics	
<ul> <li>▶ Lecture 1: Syntax + Semantics of CTL*→PVR</li> </ul>	
<ul> <li>Lecture 2: Symbolic algorithm for CTL and fair CTL</li> </ul>	
Lecture 3: Counterexamples and witnesses for fragments of CTL	
► Lecture 4: Emerson-Lei algorithm improving over the naive algorithm	
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#### part II: complexity

- Lecture 5: Boolean equation systems
- Lecture 6: Parity Games
- Lecture 7: Recursive algorithm
- Lecture 8: Small Progress Measures

#### part III: data

- - Symbolic encoding the model checking problem as a PBES
  - Redundant parameter detection and elimination
  - Instantiating to a BES and solving the BES
  - Symbolic approximation + Gauß Elimination

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# **Outlook: Selection of Research and Open Ends**

### Model Checking:

- ▶ Problem is in NP∩co-NP; what is its true complexity?
- Bigstep algorithm (=Recursive+SPM) for Parity Games had best worst-case performance when d ≪ n, viz. roughly O(n<sup>d/3</sup>) Breakthrough in 2016: guasipolynomial

Parity Games and generalisations:

- Investigate runtime complexity of special games;
- Lower bounds for algorithms from literature?
- Solve Mean and Total Payoff games via Integer Equation Systems;
- Probabilistic and quantitative verification using Rational Equation Systems

### PBES technology:

- Symmetry and confluence detection and reduction for reducing the complexity
- Abstract Interpretation and predicate abstraction



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### Control software for the Large Hadron Collider

- Hierarchical system of >25 000 communicating FSMs
- Nearly fully semi-formally described
- BDD-based analysis of a subtree consisting of:
  - 7 FSMs: 5 10<sup>6</sup> states, 24 10<sup>6</sup> transitions; +/- 1 minute
  - 9 FSMs: 800 10<sup>6</sup> states; +/- 10 minutes
     11 FSMs: 120 10<sup>9</sup> states; +/- half a day
- Dedicated verification: SAT solving techniques
- Results:
  - Approx. 5% of all FSMs suffer from livelocks (20% of the FSMs that *can* be affected)
  - Approx. 4% of all FSMs suffer from reachability issues



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# **Outlook: Applications**

### Verification for Dezyne

- Dezyne: DSL and toolsuite for modelling and generating software
- Verification of Dezyne models using FDR and, more recently, mCRL2
- Dezyne used at:
  - ASML
  - Fei
  - NSpyre
  - •



# **Outlook: Applications**

### The DIRAC grid solution used at the Large Hadron Collider beauty experiment

- cooperating distributed services
- light-weight agents delivering the workload to the Grid resources
- agents run concurrently
- State spaces of 160 10<sup>6</sup> states are no exception
- Results:
  - Livelocks
  - Race conditions
  - Dead jobs reviving (zombies)
  - ...

Internship/final projects (possibly at CERN?)/research for fun? Contact me!

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