







## **Practical Problems with Randomization**

How to analyse randomness, what distribution? Statistical tests

Human subjects are bad at creating/assessing randomness

Exploit **natural phenomena** (white noise, radioactive decay, ...) See: random.org

Need for reproducibility: seeding

Need for good statistical properties

Cryptographic protocols need unpredictability

N.B. Good statistical properties  $\neq$  Unpredictability

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## Application of Randomization in Games

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Three sources of uncertainty in game playing (can be mixed):

- 1. **Combinatorial**: full information, large number of combinations Monte Carlo methods for the board game Go: random game play
- Stochastic: fortune, neutral interfering daemon
  Markov Decision Processes, deterministic optimal play
- Strategic: hidden information, adversary with secrets
  Randomization guarantees unpredictability, prevents being exploited

Role of variance: N repetitions reduce standard deviation by  $\frac{1}{\sqrt{N}}$ 

Randomization by Software
It is notoriously hard to generate random events/numbers by software: <b>Pseudo Random Number Generator</b> (PRNG)
Linear Congruential Generator (LCG):
$X_{n+1} = (aX_n + c) \mod m$
for appropriate fixed integers $a, c, m$ ; $X_0$ is seed LCG is <i>periodic</i> , and predictable after one sample (if $a, c, m$ known)
Guideline: keep number of samples $<$ square root of the period
Mersenne Twister: seeded, period $2^{19937} - 1 \approx 43 \times 10^{6000}$ Predictable after 624 samples
See: en.wikipedia.org/wiki/Mersenne_twister
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## Summary

- Even exact algorithms are not 100% reliable when executed on real hardware, because hardware is inherently unreliable
- The longer the run time of a program, the higher the probability that something goes wrong, physically
- Sacrificing exactness, by using randomization, can lead to very efficient and still highly reliable algorithms
- Two techniques illustrated with bit-string equality protocol:
  - 1. Exploit an abundance of witnesses
  - 2. Repeat random computation to increase success probability

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