Exam type problems for homework sets 3 and 4

(not to be handed in, obviously)

Set 3: (possibly as part of some other problem)

Find a parameterization for the ellipsoid in \mathbb{R}^3 with equation

$$\left(\frac{x-x_0}{a}\right)^2 + \left(\frac{y-y_0}{b}\right)^2 + \left(\frac{z-z_0}{c}\right)^2 = 1, \qquad a, b, c > 0.$$

Set 4: Let $f : \mathbb{R}^2 \longrightarrow \mathbb{R}$ be differentiable. Show that

$$\frac{d}{dt}f(t,e^t-1)|_{t=0} = \frac{d}{dt}f(e^t-1,t)|_{t=0}.$$