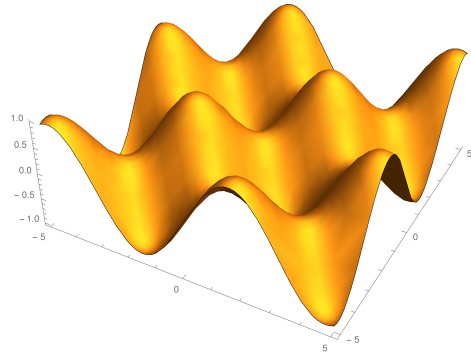


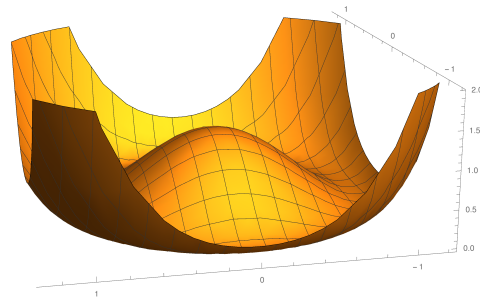
## Extrema: Examples

$$(D = \mathbb{R}^2)$$

$$f(x, y) = \sin(x) \sin(y)$$



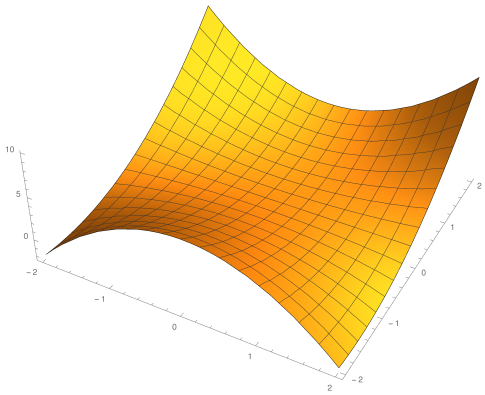
$$f(x, y) = (1 - x^2 - y^2)^2$$



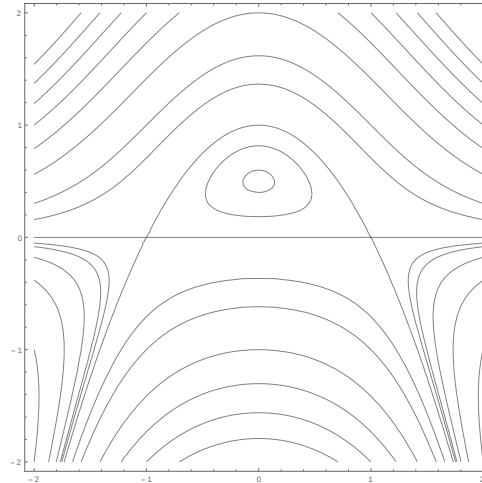
## Extrema: Examples

$$f(x, y) = x^2y + y^2 - y$$

Graph:



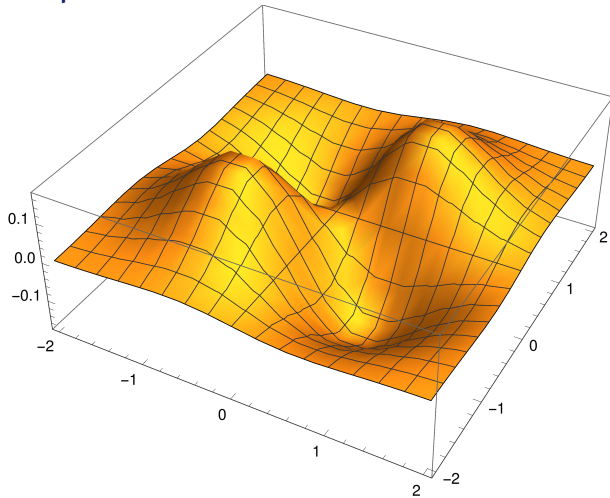
Hoogtelijnen:



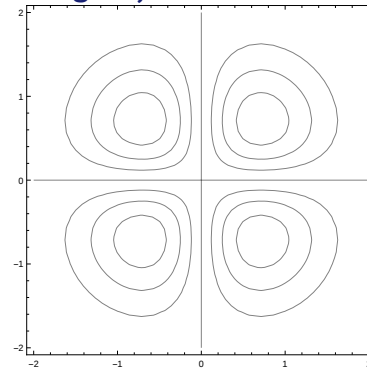
## Extrema: Examples

$$f(x, y) = xye^{-x^2-y^2}$$

Graph:



Hoogtelijnen:



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**Theorem:** Continuous functions on bounded domains including the boundary take their maximal and minimal value in some point.

Procedure to find them for differentiable functions:

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- Find the largest / smallest value among the candidates.