

# A hierarchy of SOS rule formats

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# History of the *tyft/tyxt* format



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Frits Vaandrager: “write an introduction into  $ACP_\varepsilon$ ”.

$$a \xrightarrow{a} \tau$$

$$\tau \xrightarrow{\tau} \tau$$

$$\varepsilon \xrightarrow{\surd} \delta$$

$$\frac{p \xrightarrow{a} p'}{p+q \xrightarrow{a} p'}$$

$$\frac{q \xrightarrow{a} q'}{p+q \xrightarrow{a} q'}$$

$$\frac{p \xrightarrow{a} p'}{p \cdot q \xrightarrow{a} p' \cdot q}$$

$$\frac{p \xrightarrow{\surd} p' \quad q \xrightarrow{a} q'}{p \cdot q \xrightarrow{a} q'}$$

$$\frac{Body_X \xrightarrow{a} p'}{X \xrightarrow{a} p'}$$

$$\frac{p \xrightarrow{\tau} p' \quad p' \xrightarrow{a} p''}{p \xrightarrow{a} p''}$$

$$\frac{p \xrightarrow{\tau} p' \quad p' \xrightarrow{a} p''}{p \xrightarrow{a} p''}$$

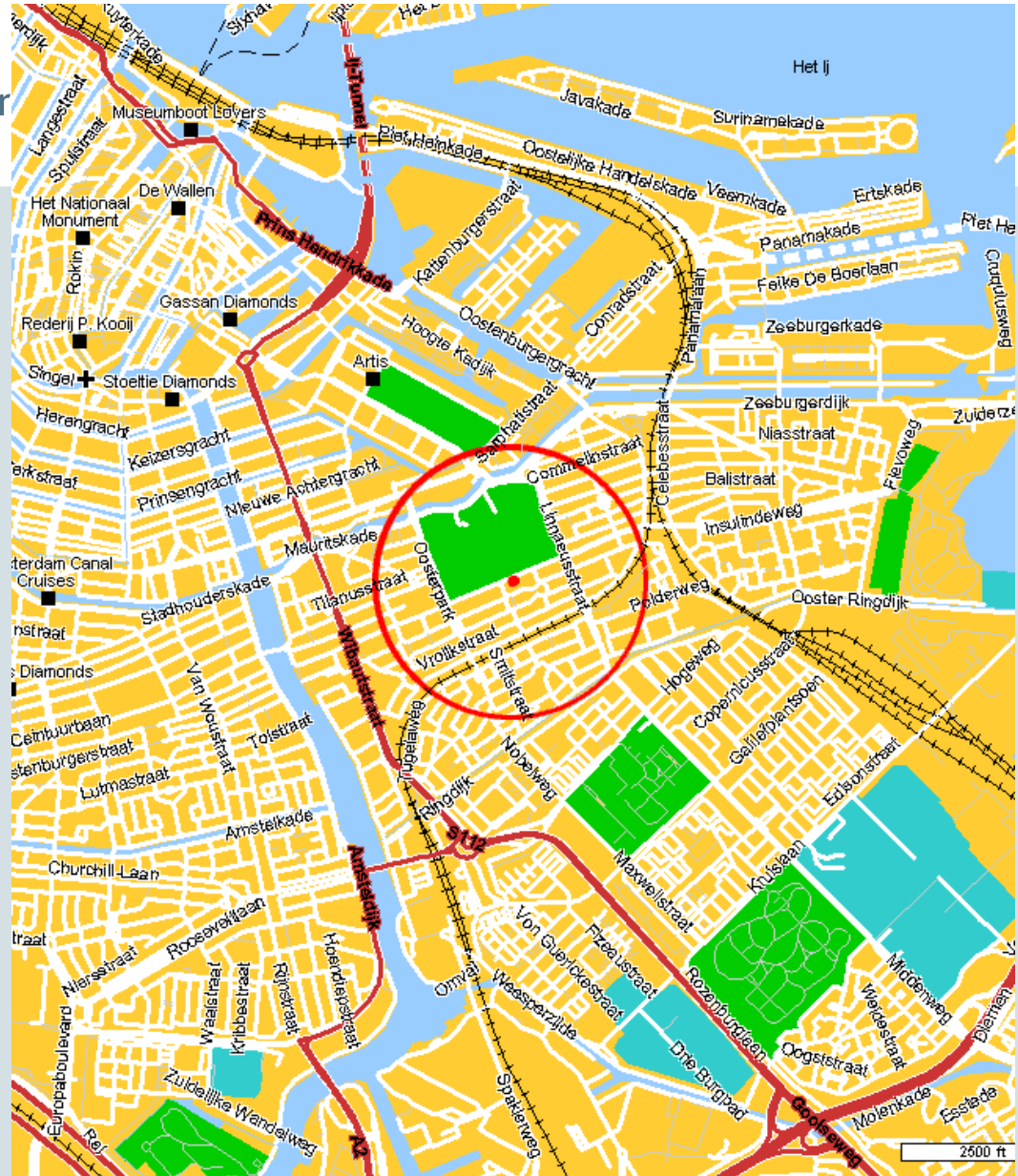
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Structured operational semantics

$$\frac{Body_X \xrightarrow{a} p'}{X \xrightarrow{a} p'}$$

$$X \xrightarrow{\tau} Body_X$$

tyft/tyxt-format



## Negative premises (priority operator)

$$\frac{p \xrightarrow{a} p' \quad \forall b > a \ p \not\xrightarrow{b}}{\theta(p) \xrightarrow{a} \theta(p')}$$

*ntyft/ntyxt-format*

*De-Simone-format*

*Bloom-Istrail-Meyer-format (BIM-format)*

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## Developments from 1990-2004

- Predicates
- Terms as labels
- Formats linked to a particular semantics
- Variable binding and substitution
- Structural congruences
- Formats for process/data pairs
- Rules with orderings
- .....

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## Predicates (BV 93, Verhoef 95)

$\varepsilon \downarrow$

$$\frac{P_0 \downarrow \quad P_1 \downarrow}{P_0; P_1 \downarrow}$$

$$\frac{P_0 \xrightarrow{a} P_0'}{P_0; P_1 \xrightarrow{a} P_0'; P_1}$$

$$\frac{P_0 \downarrow \quad P_1 \xrightarrow{a} P_1'}{P_0; P_1 \xrightarrow{a} P_1'}$$

# Terms as labels (Bernstein 98, others)

$$\frac{x \xrightarrow{[w/a]} y}{m?a.x \xrightarrow{m?w} y} \quad [prefix1]$$

$$\frac{x \xrightarrow{m!} y_1 \quad x \xrightarrow{m!*} y_2 \quad x' \xrightarrow{m?y_1} y'}{x \mid x' \xrightarrow{\tau} y' \mid y_2} \quad [par2]$$

## Variable binding/substitution

- Fokkink/Verhoef98

$$\text{send}(x, y. v^*) \xrightarrow{(x, y)} v^*$$

$$\frac{y^*[w^*/x] \xrightarrow{a} z^*}{y^* \xrightarrow{b} z^*}$$

## Structural congruences [MR05]

$$\frac{P_0 \xrightarrow{a} P_0'}{P_0 \parallel P_1 \xrightarrow{a} P_0' \parallel P_1'}$$

$$P_0 \parallel P_1 \equiv P_1 \parallel P_0$$

$$!P \equiv P \parallel !P$$

## Ordering on rules [Ulidowski & Phillips97]

$$\frac{P_0 \xrightarrow{a} P_0'}{P_0;P_1 \xrightarrow{a} P_0';P_1} > \frac{P_1 \xrightarrow{a} P_1'}{P_0;P_1 \xrightarrow{a} P_1'}$$

## Name passing/scoping (ZMP05)

$$\frac{\nabla x(Px \xrightarrow[p]{A} Qx)}{\forall x.Px \xrightarrow[p]{A} \forall x.Qx} \quad (\text{RES})$$

$$\frac{P \xrightarrow[n \rightarrow p]{\downarrow X} M \quad Q \xrightarrow[v \rightarrow p]{\uparrow X} N}{P \mid Q \xrightarrow[p]{\tau} \forall y.(My/Ny)} \quad (\text{CLOSE})$$

# Transition systems with data (MRG04)

$$\frac{\{\langle t_{pi}, t_{di} \rangle \xrightarrow{l_i} \langle t'_{pi}, t'_{di} \rangle \mid i \in I\}}{\langle t_p, t_d \rangle \xrightarrow{l} \langle t'_p, t'_d \rangle}$$

$$\frac{\{\langle t_{pi}, t_{di} \rangle \xrightarrow{l_i} \langle y_{pi}, t'_{di} \rangle \mid i \in I\}}{\langle f_p(x_{p0}, \dots, x_{pn-1}), t_d \rangle \xrightarrow{l} \langle t'_p, t'_d \rangle}$$

process-tyft

# General



# Specific

## Results

- Congruences for various equalities and preorders
- Conservative extensions
- Induced trace congruences
- Existence of semantics (negative premises)
- Generation of complete axiomatisations
- Generators for simulators
- Various: non-interference; semi-stochasticity;

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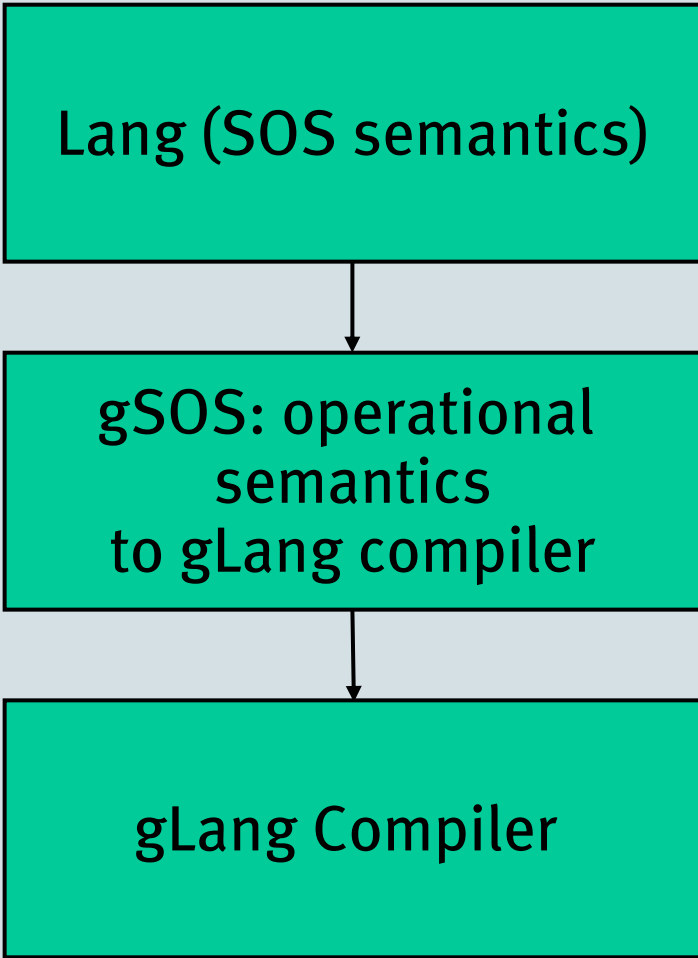
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## The *super* rule format

- Terms: simply typed  $\lambda$ -calculus?
- Terms as labels!
- Freshness  $\nabla$ ,  $a\#t$

# Compiler generators from SOS



Lang = Java; C#; C++;  $\pi$ -calculus; mCRL2; Domain and aspect languages;

cf. lex/yacc

Axioms for optimisation

Performance must be comparable to gcc

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