Towards Verified Construction of Correct and Optimised GPU Software

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Abstract

Techniques are required that support developers to produce GPU software that is both functionally correct and highperforming. We envision an integration of push-button formal verification techniques into a Model Driven Engineering workflow. In this paper, we present our vision on this topic, and how we plan to make steps in that direction in the coming five years.

CCS Concepts: • Software and its engineering \rightarrow Software verification and validation; Software functional properties; System description languages.

Keywords: GPU software, formal verification, model transformation, code generation

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1 Introduction

The use of *graphics processors* (GPUs) for general purpose computing has greatly impacted the computational capabilities regarding linear algebra (e.g., matrix-vector multiplication [44, 88]), computational biology (e.g., genomics [85] and genetic network reconstruction [16]), statistics [63], physics (e.g., fluid dynamics [9]), image processing [64], formal verification [6–8, 33, 87, 89, 92, 93], and machine learning (deep learning [57]). However, to effectively use GPUs, expert knowledge is required about the hardware characteristics, and even then, software development can be

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time-consuming and frustrating. Proper techniques to make the development and maintenance of GPU software more insightful and less prone to introduce bugs, while helping the developer to introduce performance optimisations, are lacking [43, 50, 73]. The existence of such tools would make GPU computing a far more attractive option for most software developers. In the current paper, we outline our vision to integrate *formal verification techniques* [5, 12, 26, 38, 70] into a *Model Driven Engineering* (MDE) [17, 75] workflow, to provide suitable GPU software development tools. It is crucial that those techniques do not require expert knowledge on formal verification, to make them usable for the average software developer.

In MDE, one reasons about the system under development in terms of a model written in a Domain-Specific Language (DSL) [41, 65]. *Model transformations* are applied on models, for instance, to add more information, to rewrite the model in a different DSL, or to generate source code.

MDE enables a very structured way of software development, and improves flexibility: the model can be updated, and code can be regenerated and optimised at any time. However, MDE currently provides no guarantees that the resulting software will be correct and efficient, i.e. a) that it does what it is supposed to do, and b) that it does this while realising the full potential of the hardware it is running on.

2 Our Envisioned MDE Workflow

In the coming five years, in the ChEOPS project¹, we plan to use formal verification techniques to establish in every step of an MDE workflow that the produced GPU system will be functionally correct and preserve the semantics of the model. First, a model is constructed that describes the desired functionality using an appropriate DSL. This model is formally verified to determine whether it correctly addresses the intended functionality. Next, a GPU implementation of the system is generated. Verification of such an implementation with a code verification tool, such as VerCors [15] and VeriFast [78], can be very time-consuming and typically requires a formal verification expert. Therefore, the approach we plan to follow is to automatically annotate the code with the semantics of the model, such that those tools can be used with the push of a button. Recently, we have applied this

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¹http://cheops.win.tue.nl.

approach to achieve verified generation of multi-threaded software [86]. Finally, in a number of steps, the produced source code can be transformed to optimise it for specific GPU hardware. In these steps, annotations will be refined along with the code and code verification will be reapplied.

To achieve this, a number of topics need to be addressed.

2.1 Specifying and Verifying GPU Program Models

In the literature, many DSLs have been proposed to specify parallel systems, some of which targeting GPU systems, e.g. [2, 31, 34, 36, 39, 47, 53, 59, 81]. The ability to produce high-performance GPU systems is an obvious criterion, but much less attention has been given to the verifiability of the produced models. We believe that DSLs are needed that allow reasoning at an abstraction level that is not too high, to be able to still address the relevant behaviour, but also not too low, since that would make verification infeasible. Developers also need to be supported in specifying desired functional properties. Various proposals have been made for the specification of functional properties of parallel systems, for instance to use some form of message sequence charts [18, 25, 54, 55, 61]. However, it is yet to be determined whether such approaches are suitable for GPU systems.

To verify models, we plan to use model checking [5, 26, 89, 93], because of its push-button nature. Previously, GPU programs have been model checked w.r.t. specific properties such as data races and pointer safety [66], but no experience has been reported on checking whether models of GPU software satisfy user-defined functional properties.

2.2 Verified Generation of Code by Means of Model-to-Code Transformations

As GPU code will be produced by using model-to-code transformations, it is crucial to establish that those transformations preserve the semantics of the source model.

Existing approaches, such as [1, 13, 24, 29, 35, 71, 76, 79, 80, 82–84], are not general enough for our purpose; they do not directly support the development of GPU software (or other types of parallel software). Moreover, they do not achieve a push-button approach. For model-to-model transformations, we have developed such techniques [32, 90, 91], but model-to-code transformations pose extra challenges related to the target hardware and programming language.

By generating annotated code, existing tools such as Open-JML [27], KeY [3] and Dafny [58] can be applied. Originally aimed at sequential code, these techniques are currently extended to support concurrent and parallel software. On the one hand, there is a line of very active research defining highly advanced program logics for fine-grained concurrency such as CAP [37], TaDa [28], and Iris [52, 56]. On the other hand, there are tools that support the verification of concurrent and parallel programs, such as Ver-Cors [4, 14, 15, 30, 74] (using Viper [67]), and VeriFast [78]. Techniques specifically designed for the analysis of GPU software, such as GPUverify [10, 11] and PUG [60], address crucial correctness issues, such as thread divergence and data races, but they do not support checking user-defined functional requirements.

Regarding the generation of program annotations, we observe that many auxiliary annotations can be generated automatically. In particular, there exists a large body of literature on invariant generation, see e.g., [42, 46, 51, 72, 77]. However, most of those techniques are not applied in program verification, as they do not always match directly with what is needed. For instance, for program verification, one often needs invariants that express properties about arrays or other kinds of data types, but hardly any techniques to automatically generate those have been developed. We believe that this is an important topic to address.

2.3 Correct Transformation of Source Code to Achieve High-Performance Software

When focussing on correctness, performance should not be ignored, especially when developing software for parallel hardware architectures. The main purpose of DSLs is to allow developers to reason at a comfortably high level of abstraction about the intended functionality of the system. Performance-related aspects necessarily require a more technical, low-level view, since optimisations involve closely mapping the software to the hardware. This discrepancy means that an implementation generated from a DSL model is typically not optimised for performance, and additional transformations at the program level are necessary.

In the literature, a large collection of program transformations to improve performance of GPU applications is available, see e.g. [22, 48, 94]. Only in a few cases, formal correctness of these is addressed, for instance in [68].

We will work on producing GPU programs that come with detailed annotations describing which parts of the memory are accessed and changed by which parts of the code (see [49] for preliminary ideas). Besides making a program verifiable, these annotations will also provide valuable information to determine which transformations can be applied to optimise the program. Work on algorithmic classification, which classifies a given program and based on that suggests to apply certain optimisations, is relevant here [19-21, 23, 40, 45, 69]. Moreover, we observe that the information in the annotations can be used to speed up the auto-tuning process, i.e., the process to identify which program configuration achieves the best performance. Optimal tuning can be a timely process, and the use of information to reduce the state space for tuning can have substantial impact [62]. Because of the very precise information available from our program annotations, we believe that we can substantially reduce the overhead of this process. Using detailed program annotations for both verification and optimisation is very new, and we strongly believe that it can be used effectively to produce high-quality GPU software.

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