

## Coercion-Resistant Remote Voting Using Decryption Mixes

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## Remote Voting

- Clear interest
  - SERVE, Debian (devotee), program committees, etc.
- CIVS: Condorcet Internet Voting Service
  - <http://www5.cs.cornell.edu/~andru/civs/>
  - Offers security guarantees:
    - Whether/how a voter votes remains secret, even if server storage compromised
    - *But assuming trusted server software, and without verifiability*
  - Users have run ~100 elections with 10–1700 voters
- Redesign to get **verifiability** and **coercion resistance** without a trusted server

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## Trust Model

- We **have** to trust client software
  - Implementation of CIVS2 in Jif
    - Java + Information Flow
    - Check that information flows obey confidentiality and integrity policies
- Move rest of trust into:
  - Cryptography
  - Anonymous channel
  - Set of tellers

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## Prêt à Voter (PAV)

- [Chaum, Ryan, Schneider, {4, 0} days ago]
- Uses decryption mix and auditing to remove trust in much of mechanism
- But designed for *supervised voting*, not remote
  - Authentication and handling of ballots rely on trusted officials, booth, and machine

Problem 1: Adapt PAV to Internet voting

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## Ranked Voting Methods

- Voters submit ordering of candidates:

Vanilla	4
Chocolate	1
Strawberry	3
Cookie dough	2
Mint chocolate chip	5

- Captures more information about “the will of the people” than binary voting methods
- Condorcet, STV/IRV, Borda, ...

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## Covert Channel in Rankings

- Low-order rankings create a covert channel
  - Voter can encode identity using channel

Vanilla	X
Chocolate	X
Strawberry	X
Cookie dough	X
Mint chocolate chip	1

} 4! completions

- Coercion intrinsically possible
  - Many ranked methods require access to the individual votes cast
  - Most schemes, including PAV, make the votes public

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## Condorcet Methods

- Benefits:
  - Usually do not require individual ballots
  - Many argue they produce superior results (at least over FPTP)
- *Condorcet winner* (CW) is the candidate who would defeat every other candidate in a one-on-one plurality vote
  - Chocolate beats Vanilla 60-40
  - Chocolate beats Mint 90-10
 } Chocolate is CW
- Strongly democratic: majority rule is enforced
- Resistant to strategic voting
  - Voters have strong incentive to vote true preferences

Problem 2: Adapt PAV to Condorcet methods

## Overview

Problem 1: Adapt PAV to Internet voting

- Eliminate trusted supervision
  - Ballot distribution
  - Authentication

Problem 2: Adapt PAV to Condorcet methods

- Eliminate covert channel in ranked ballots

## Condorcet Ballots

- Simple: Decompose rankings into a  $C \times C$  binary matrix
  - $C$  = number of candidates
  - Cell  $(i,j) = 1$  if voter prefers candidate  $i$  to  $j$ , 0 otherwise
- Treat each cell as a separate vote
  - Each with its own unique ballot and onion
  - Voter casts  $O(C^2)$  0/1 votes
- Engineering ballot forms
  - No longer PAV's cyclic ordering of fixed set of candidates
  - Let  $\text{onion}(D)$  be an onion with innermost layer  $D$
  - Ballot for  $i$  vs.  $j$  has  $\text{onion}(i,j)$
  - Audit sets of ballots for well-formedness

S,M	
	g3R04

## Tallying Ballots



## Tallying Ballots

- Compute a sum matrix from final column of mix
  - Run any *additive/summable* algorithm for CW
- Coercion resistant:
  - Identifying low-order preferences requires identifying the set of votes from a voter
  - But PAV's decryption mix anonymizes *each* vote in final column
  - Sets not identifiable, so neither are low-order preferences

## Ballot Handling

- Problem: LHS+onion of ballot reveals too much
  - Must prevent everyone (except voter) from learning map from LHS to onion
    - Distributor(s) of ballots
    - Creator(s) of ballots
- Our solution: conceal LHS, reveal only to voter

## Ballot Distribution

- Assume:
  - $E(D; K)$  is encryption of  $D$  with  $K$
  - $K_{VS}$  is an ElGamal public key for the voting system
  - Private key  $k_{VS}$  is split among all tellers

$E(i,j; K_{VS})$	
	onion( $i,j$ )

- No one knows the map from encrypted LHS to decrypted candidates, i.e. from  $E(i,j; K_{VS})$  to  $\langle i,j \rangle$

## Ballot Distribution

- Anyone can be permitted to see the ballot, but only voter can learn the LHS decryption
- Distributed reencryption [Zhou et al. '05]
  - Transform  $E(D; K_A)$  to  $E(D; K_B)$ 
    - Performed by servers who share  $k_A$
    - Nowhere does  $D$  appear as plaintext
  - Voter has  $E(i,j; K_{VS})$  reencrypted to  $E(i,j; K_V)$
  - But requires  $2f+1$  servers/tellers

## Ballot Creation

- Goal: Create  $E(i,j; K_{VS})$ , onion( $i,j$ )
- No single entity can be trusted to create ballots
  - Would learn decrypted candidate map
- Encrypted candidate pair needs to be transformed; we use blinding
  - Ballots created in large sets
  - Each ballot clerk adds a blinding factor and shuffles set
  - By homomorphic property, voter can use distributed reencryption to strip off blinds

## Authentication

- Before system can distribute a ballot, must ensure voter is authorized in election
- So voter must authenticate
  - Anything voter knows can be demanded by coercer
  - So like [Juels, Catalano, Jakobsson], we need to enable voter to lie about what he knows
- One idea: Capability is:
  - $$\text{onion}(S(\text{"valid"}, \text{nonce}; k_{VS}))$$
    - Attach capability to each vote:  $\langle vc, 0/1, o \rangle$
    - In final column of mix, capability is stripped to  $S(\text{"valid"}, \text{nonce})$
    - Voter can lie by inventing fake capabilities
    - In final column, can detect **anonymized** fakes

## Authentication

- Voter can:
  - Give coercer fake capability and let coercer vote
  - Submit any vote (including random) under fake capability
  - Abstain from casting a vote with a fake capability
- Problem:
  - Registrar who creates and distributes capabilities has to be trusted to forget valid capabilities, map from voter to capability issued, etc.
  - Need a distributed onion construction
- Voters must use (sufficiently) anonymous channel to request ballots, submit votes

## Conclusions

- Encode ranked ballots in PAV onions
  - (Additive) Condorcet methods
- Eliminated (most of) trusted supervision
  - Ballot creation
  - Ballot distribution
  - (Authentication)

## Future Work

- Implementation of CIVS2
  - Jif: What policies can be expressed?
- How can we do anonymous, at-most-once authentication?
  - Distributed onion construction?
- Can ballot distribution failure model be improved using distributed decryption?
- Can we prevent ballot stuffing?