Consider the functions

$$f(x_1, x_2, x_3) = (x_1 + x_2)(x_1 + x_3)$$
$$g(x_1, x_2, x_3) = (x_1 + x_2) - (x_1 + x_3)$$
$$h(x_1, x_2, x_3) = (x_1 + x_2) / (x_1 + x_3)$$

### Question: Which of these functions are linear?

- A. None.
- B. Only  $f(x_1, x_2, x_3)$
- C. Only  $g(x_1, x_2, x_3)$
- D. Only  $h(x_1, x_2, x_3)$

Consider the functions

$$f(x_1, x_2, x_3) = |x_1|$$
  
$$g(x_1, x_2, x_3) = \log(x_1 + x_2 + x_3)$$

Question: Which of these functions are linear?

- A. Neither.
- B. Only  $f(x_1, x_2, x_3)$
- C. Only  $g(x_1, x_2, x_3)$
- D. Both.

Consider the constraints

(1) 
$$x_1 + x_2 + x_3 \cdot x_4 \leq 50$$
  
(2)  $x_1 + x_2 + x_3 \leq x_1^2$   
(3)  $x_1 + x_2 + x_3 < 50$ 

Question: Which of these constraints are linear?

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- A. None.
- B. Only (1)
- C. Only (2)
- D. Only (3)

Consider the constraints

(1) 
$$x_1 + x_2 + x_3 \neq 50$$
  
(2)  $x_1 + x_2 + x_3 = 3x_1 + \log(27)$   
(3)  $1/(x_1 + x_2 + x_3) \geq 250$ 

Question: Which of these constraints are linear?

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- A. None.
- B. Only (1)
- C. Only (2)
- D. Only (3)

Consider the variable definitions

(1) 
$$x_1, x_2, x_3 \in \mathbb{Q}$$
  
(2)  $x_1, x_2 \in \mathbb{R} - \{0\}$   
(3)  $x_1, x_2 \in \mathbb{R}; x_3 \in \{0, 1, 3\}$ 

Question: Which of these definitions agree with our standard LP problem?

}

- A. None.
- B. Only (1)
- C. Only (2)
- D. Only (3)

Consider the variable definitions

(1) 
$$x_1, x_2, x_3 \in \mathbb{R} - (-\infty, 0]$$
  
(2)  $x_1, x_2 \in \mathbb{R} - (1, 2)$   
(3)  $x_1, x_2, x_3 \in [0, 3]$ 

Question: Which of these definitions agree with our standard LP problem?

- A. None.
- B. Only (1)
- C. Only (2)
- D. Only (3)

$$\begin{array}{rll} \max & 4x_1 + 8x_2 \\ s.t. & x_1 - x_2 \leq -1 \\ & 2x_1 - x_2 \leq 5 \\ -3x_1 - x_2 \leq -3 \\ & 2x_1 + x_2 \leq -3 \\ & 2x_1 + x_2 \leq 7 \\ & 10x_1 + x_2 \leq 20 \\ & x_1, & x_2 \geq 0 \end{array}$$

Question: Which of the following vectors is feasible?

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A. 
$$x = (0,0)$$
  
B.  $x = (2,3)$   
C.  $x = (1,7)$   
D.  $x = (1,4)$ 

$$\begin{array}{ll} \max & x_1 + x_2 \\ s.t. & x_1 + x_2 & \leq 8 \\ & 0 \leq x_1, x_2 \leq 6 \end{array}$$

### Question: This LP

- A. is infeasible
- B. is unbounded
- C. has infinitely many solutions

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$$\max x_1 + 2x_2 \\ s.t. x_1 + x_2 \le 8 \\ 0 \le x_1, x_2 \le 6$$

### Question: This LP

- A. is infeasible
- B. is unbounded
- C. has infinitely many solutions

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$$\max x_1 + 2x_2 \\ s.t. x_1 + x_2 \le 8 \\ 0 \le x_1, x_2 \le 1$$

### Question: This LP

- A. is infeasible
- B. is unbounded
- C. has infinitely many solutions

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$$\max x_1 + x_2$$
  
s.t.  $x_1 - x_2 \leq 8$   
 $x_1 - x_2 \geq 4$   
 $0 \leq x_1, x_2$ 

#### Question: This LP

- A. is infeasible
- B. is unbounded
- C. has infinitely many solutions

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min 
$$2x_1 + 3x_2$$
  
s.t.  $x_1 - x_2 \leq 8$   
 $x_1 - x_2 \geq 4$   
 $0 \leq x_1, x_2$ 

#### Question: This LP

- A. is infeasible
- B. is unbounded
- C. has infinitely many solutions

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min 
$$2x_1 + 3x_2$$
  
s.t.  $2x_1 - x_2 \ge 8$   
 $x_1 + x_2 \ge 13$   
 $0 \le x_1 \le 6$   $0 \le x_2 \le 34$ 

#### Question: This LP

- A. is infeasible
- B. is unbounded
- C. has infinitely many solutions

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### Question: This LP

- A. is infeasible
- B. is unbounded
- C. has infinitely many solutions

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$$\max x_1 + x_2 + x_3 \\ s.t. x_1 + x_2 - 2x_3 \leq 6 \\ x_1 - 2x_2 + x_3 \leq 7 \\ -2x_1 + x_2 + x_3 \leq 8 \\ 9 \leq x_1, x_2, x_3 \\ \end{array}$$

#### Question: This LP

- A. is infeasible
- B. is unbounded
- C. has infinitely many solutions

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### TRUE or FALSE?

There exists an LP that has exactly four optimal solutions that are basic feasible (= corner points of the feasible region).

- A. True
- B. False

Solve the following LP with the Simplex method:

	Ζ	<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	$s_1$	<i>s</i> <sub>2</sub>	<i>s</i> 3	b
Ζ	1	-2	-1	-1	0	0	26
<i>s</i> <sub>1</sub>	0	4	4	1	0	0	6
<i>s</i> <sub>2</sub>	0	5	6	1	1	0	16
<i>s</i> 3	0	7	4	1	0	1	10

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Question: Which statement is true?

- A. This LP is infeasible
- B. The optimal objective value is 32
- C. The optimal solution has  $x_2 = 8$
- D. The optimal solution has  $x_2 = 9$

Solve the following LP with the Simplex method:

Question: Which statement is true?

- A. This LP is infeasible
- B. The optimal solution has  $x_2 = 0$
- C. The optimal solution has  $x_2 = 1/10$
- D. The optimal solution has  $x_2 = 1/5$

Solve the following LP with the Simplex method:

	Z	<i>x</i> <sub>1</sub>	<i>x</i> <sub>2</sub>	$s_1$	<i>s</i> <sub>2</sub>	<i>s</i> 3	Ь
Ζ	1	-1	-1	0	0	0	0
<i>s</i> <sub>1</sub>	0	3	5	1	0	0	90
<b>s</b> 2	0	9	5	0	1	0	180
<i>s</i> 3	0	0	1	0	0	1	15

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Question: Which statement is true?

- A. This LP is infeasible
- B. The optimal objective value is 32
- C. The optimal solution has  $x_2 = 8$
- D. The optimal solution has  $x_2 = 9$

Solve the following LP with the Simplex method: max  $5x_1 + 6x_2 + 9x_3 + 8x_4$  *s.t.*  $x_1 + 2x_2 + 3x_3 + x_4 \le 5$   $x_1 + x_2 + 2x_3 + 3x_4 \le 3$  $x_1, x_2, x_3, x_4 \ge 0$ 

Question: Which statement is true?

- A. The optimal objective value is 15
- B. The optimal objective value is 17
- C. The optimal objective value is 19
- D. The optimal objective value is 21