## Clicker \#A. 1

|  | $Z$ | $x_{1}$ | $x_{2}$ | $x_{3}$ | $s_{1}$ | $s_{2}$ | $s_{3}$ | $b$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | ---: |
| $Z$ | 1 | -9 | -5 | -1 | 0 | 0 | 0 | 80 |
| $s_{1}$ | 0 | 3 | 4 | 0 | 1 | 0 | 0 | 90 |
| $s_{2}$ | 0 | -9 | 4 | 0 | 0 | 1 | 0 | 180 |
| $s_{3}$ | 0 | 0 | -3 | -1 | 0 | 0 | 1 | 15 |

## Question: This LP

A. is infeasible
B. is unbounded
C. has infinitely many optimal solutions
D. has a unique optimal solution

## Clicker \#A. 2

|  | $Z$ | $x_{1}$ | $x_{2}$ | $x_{3}$ | $s_{1}$ | $s_{2}$ | $s_{3}$ | $b$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | ---: |
| $Z$ | 1 | 3 | 0 | 7 | 0 | 0 | 0 | 0 |
| $s_{1}$ | 0 | 3 | 4 | 0 | 1 | 0 | 0 | 90 |
| $s_{2}$ | 0 | -9 | 4 | 0 | 0 | 1 | 0 | 180 |
| $s_{3}$ | 0 | 0 | -3 | -1 | 0 | 0 | 1 | 15 |

## Question: This LP

A. is infeasible
B. is unbounded
C. has infinitely many optimal solutions
D. has a unique optimal solution

## Clicker \#A. 3

|  | $Z$ | $x_{1}$ | $x_{2}$ | $x_{3}$ | $s_{1}$ | $s_{2}$ | $s_{3}$ | $b$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | ---: |
| $Z$ | 1 | -3 | 8 | 0 | 0 | 0 | 0 | 54 |
| $s_{1}$ | 0 | 3 | 4 | 0 | 1 | 0 | 0 | 90 |
| $s_{2}$ | 0 | -9 | 4 | 0 | 0 | 1 | 0 | 80 |
| $s_{3}$ | 0 | 5 | -3 | 0 | 0 | 0 | 1 | 255 |

## Question: This LP

A. is infeasible
B. is unbounded
C. has infinitely many optimal solutions
D. has a unique optimal solution

## Clicker \#A. 4

|  | $Z$ | $x_{1}$ | $x_{2}$ | $x_{3}$ | $s_{1}$ | $s_{2}$ | $s_{3}$ | $b$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | ---: |
| $Z$ | 1 | 3 | 0 | 17 | 0 | 9 | 0 | 54 |
| $s_{1}$ | 0 | 3 | 0 | 1 | 1 | -2 | 0 | 90 |
| $x_{2}$ | 0 | -9 | 1 | 1 | 0 | -1 | 0 | 80 |
| $s_{3}$ | 0 | 5 | 0 | 0 | 0 | 0 | 1 | 255 |

Question: This LP
A. is infeasible
B. is unbounded
C. has infinitely many optimal solutions
D. has a unique optimal solution

## Clicker \#A. 5

|  | $Z$ | $x_{1}$ | $x_{2}$ | $x_{3}$ | $s_{1}$ | $s_{2}$ | $s_{3}$ | $b$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | ---: |
| $Z$ | 1 | 3 | 0 | 17 | 1 | 9 | 0 | 54 |
| $s_{1}$ | 0 | 3 | 0 | 0 | 1 | -2 | 0 | 90 |
| $x_{2}$ | 0 | -9 | 1 | 0 | 0 | -1 | 0 | 80 |
| $s_{3}$ | 0 | 5 | 0 | 0 | 0 | 0 | 1 | 255 |

Question: This LP
A. is infeasible
B. is unbounded
C. has infinitely many optimal solutions
D. has a unique optimal solution

## Clicker \#A. 6

|  | $Z$ | $x_{1}$ | $x_{2}$ | $x_{3}$ | $s_{1}$ | $s_{2}$ | $s_{3}$ | $b$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $Z$ | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| $s_{1}$ | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| $x_{2}$ | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| $s_{3}$ | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |

## Question: This LP

A. is infeasible
B. is unbounded
C. has infinitely many optimal solutions
D. has a unique optimal solution

## Clicker \#B. 1

|  | $Z$ | $x_{1}$ | $x_{2}$ | $x_{3}$ | $s_{1}$ | $s_{2}$ | $a_{1}$ | $a_{2}$ | $b$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $Z$ | 1 | 1 | 0 | 3 | 0 | 0 | $2+M$ | $M$ | $16-M$ |
| $s_{2}$ | 0 | 5 | 0 | 3 | 0 | 1 | 3 | -1 | 4 |
| $s_{1}$ | 0 | -1 | 0 | -1 | 1 | 0 | -1 | 0 | 2 |
| $x_{2}$ | 0 | 2 | 1 | 1 | 0 | 0 | 1 | 0 | 8 |

Question: This LP (specified by tableau for Big-M method)
A. is infeasible
B. is unbounded
C. has an optimal solution
D. none of the above

## Clicker \#B. 2

|  | $Z$ | $x_{1}$ | $x_{2}$ | $x_{3}$ | $s_{1}$ | $s_{2}$ | $a_{1}$ | $a_{2}$ | $b$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $Z$ | 1 | $M$ | 0 | 3 | 0 | 0 | $2+M$ | $M$ | 26 |
| $s_{2}$ | 0 | 5 | 0 | 3 | 0 | 1 | $3+M$ | -1 | 4 |
| $s_{1}$ | 0 | -1 | 0 | -1 | 1 | 0 | $-1+M$ | 0 | 2 |
| $x_{2}$ | 0 | 2 | 1 | 1 | 0 | 0 | $1+M$ | 0 | 8 |

Question: This LP (specified by tableau for Big-M method)
A. is infeasible
B. is unbounded
C. has an optimal solution
D. none of the above

## Clicker \#B. 3

|  | $Z$ | $x_{1}$ | $x_{2}$ | $x_{3}$ | $s_{1}$ | $s_{2}$ | $a_{1}$ | $a_{2}$ | $b$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $Z$ | 1 | 1 | 0 | 3 | 0 | 0 | $2+M$ | $M$ | -65 |
| $s_{2}$ | 0 | 5 | 0 | 3 | 0 | 1 | 3 | -1 | 4 |
| $s_{1}$ | 0 | -1 | 0 | -1 | 1 | 0 | -1 | 0 | 2 |
| $x_{2}$ | 0 | 2 | 1 | 1 | 0 | 0 | 1 | 0 | 8 |

Question: This LP (specified by tableau for Big-M method)
A. is infeasible
B. is unbounded
C. has an optimal solution
D. none of the above

## Clicker \#B. 4

|  | $W$ | $x_{1}$ | $x_{2}$ | $x_{3}$ | $s_{1}$ | $s_{2}$ | $a_{1}$ | $a_{2}$ | $b$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $W$ | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 14 |
| $x_{1}$ | 0 | 1 | 0 | 3 | 0 | 1 | 3 | 1 | 4 |
| $s_{1}$ | 0 | 0 | 0 | -2 | 1 | 1 | 2 | 1 | 2 |
| $x_{2}$ | 0 | 0 | 1 | -1 | 0 | -5 | 2 | 2 | 4 |

Question: This LP (tableau $=$ end of 1st phase in 2-phase method)
A. is infeasible
B. is unbounded
C. has an optimal solution
D. none of the above

## Clicker \#B. 5

|  | $W$ | $x_{1}$ | $x_{2}$ | $x_{3}$ | $s_{1}$ | $s_{2}$ | $a_{1}$ | $a_{2}$ | $b$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $W$ | 1 | 0 | 0 | 0 | 0 | 0 | 5 | 3 | -4 |
| $x_{1}$ | 0 | 1 | 0 | 3 | 0 | 1 | 3 | 1 | 4 |
| $s_{1}$ | 0 | 0 | 0 | -2 | 1 | 1 | 2 | 1 | 7 |
| $x_{2}$ | 0 | 0 | 1 | -1 | 0 | -5 | 2 | 2 | 4 |

Question: This LP (tableau $=$ end of 1st phase in 2-phase method)
A. is infeasible
B. is unbounded
C. has an optimal solution
D. none of the above

## Clicker \#C. 1

In the primal LP, the goal is to minimize.
The optimal objective value is $\operatorname{Opt}(p)$.
In the dual LP, the goal is to maximize.
There is a feasible solution with value Feas $(d)$

Question: How many of the following three cases can actually occur?

- $\operatorname{Opt}(p)=1 \quad$ and $\quad \operatorname{Feas}(d)=3$
- $\operatorname{Opt}(p)=2$ and $\operatorname{Feas}(d)=2$
- $\operatorname{Opt}(p)=3$ and $\operatorname{Feas}(d)=1$
A. 0
B. 1
C. 2
D. 3


## Clicker \#C. 2

$$
\begin{aligned}
& \max Z=3 x_{1}+5 x_{2} \\
& \text { s.t. } \\
& \begin{aligned}
x_{1}-3 x_{2} & \geq 4 \\
-x_{1}+2 x_{2} & =12 \\
3 x_{1}+2 x_{2} & \leq 18 \\
x_{2} & \geq 0
\end{aligned}
\end{aligned}
$$

Question: The dual of this LP contains
A. $3 y_{1}+5 y_{2} \leq 4$ and $y_{1} \geq 0$
B. $y_{1}-y_{2}+3 y_{3} \leq 3$ and $y_{2} \geq 0$
C. $y_{1}-y_{2}+3 y_{3}=3$ and $y_{1}$ free
D. $-3 y_{1}+2 y_{2}+2 y_{3} \geq 5$ and $y_{3} \geq 0$

## Clicker \#C. 3

$$
\begin{aligned}
& \min Z=3 x_{1}+5 x_{2} \\
& \text { s.t. } \\
& \begin{aligned}
x_{1}-x_{2} & \geq 4 \\
-x_{1}+x_{2} & =4 \\
x_{1}+2 x_{2} & \leq 4 \\
x_{1}, & x_{2}
\end{aligned}
\end{aligned}
$$

Question: The dual of this LP contains
A. $y_{1}-y_{2}+y_{3}=3$ and $y_{2} \geq 0$
B. $y_{1}-y_{2}+y_{3} \leq 3$ and $y_{1} \leq 0$
C. $y_{1}-y_{2}+y_{3} \leq 3$ and $y_{3} \leq 0$
D. $y_{1}-y_{2}+y_{3} \geq 3$ and $y_{2}$ free

## Clicker \#C. 4

Consider a primal LP with

- 5 free variables $x_{1}, \ldots, x_{5}$
- 3 variables $x_{6}, x_{7}, x_{8} \geq 0$
- 3 constraints of type $\leq b_{i}$
- 4 constraints of type $\geq b_{i}$
- 5 constraints of type $=b_{i}$
- goal $=$ min

Question: The dual of this LP contains
A. 3 free variables and 4 constraints of type $\leq c_{i}$
B. 5 free variables and 4 constraints of type $\geq c_{i}$
C. 5 free variables and 5 constraints of type $=c_{i}$
D. 3 free variables and 3 constraints of type $=c_{i}$

## Clicker \#D. 1

## TRUE or FALSE?

There exists an LP that is equal to its dual.
A. True
B. False

