

## Clicker #A.1

	Z	$x_1$	$x_2$	$x_3$	$s_1$	$s_2$	$s_3$	$b$
Z	1	0	5	0	2	7	0	-14
$x_1$	0	1	-2	0	1	-5	0	9
$x_3$	0	0	4	1	4	1	0	18
$s_3$	0	0	-3	0	9	0	1	5

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**Question:** The optimal solution for the dual of this LP has

- A.  $y_1 = 0$  and  $s_3 = 0$
- B.  $y_3 = 0$  and  $y_1 = 2$
- C.  $y_2 = 0$  and  $y_1 = 2$
- D.  $y_1 = 0$  and  $y_2 = 7$

## Clicker #A.2

	$Z$	$x_1$	$x_2$	$x_3$	$s_1$	$s_2$	$s_3$	$b$
$Z$	1	0	5	0	2	7	0	-32
$x_1$	0	1	-2	0	1	-5	0	9
$x_3$	0	0	0	1	4	1	0	18
$s_3$	0	0	-3	0	9	0	1	5

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**Question:** The dual of this LP

- A. is infeasible
- B. is unbounded
- C. has optimal objective value 32
- D. has optimal objective value -32

## Clicker #A.3

	$Z$	$x_1$	$x_2$	$x_3$	$s_1$	$s_2$	$s_3$	$b$
$Z$	1	0	-5	0	2	7	0	-14
$x_1$	0	1	-2	0	1	-5	0	9
$x_3$	0	0	0	1	4	1	0	18
$s_3$	0	0	-3	0	9	0	1	5

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**Question:** The dual of this LP

- A. is infeasible
- B. is unbounded
- C. has optimal objective value 14
- D. has optimal objective value -14

## Clicker #A.4

	$Z$	$x_1$	$x_2$	$x_3$	$s_1$	$s_2$	$s_3$	$b$
$Z$	1	3	0	17	1	9	0	29
$s_1$	0	2	0	5	1	-2	0	58
$x_2$	0	-9	1	3	0	-1	0	80
$s_3$	0	5	0	1	0	0	1	255

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**Question:** The dual of this LP

- A. is infeasible
- B. is unbounded
- C. has optimal objective value 29
- D. has optimal objective value  $-29$

# Clicker #B.1

$$\begin{array}{rclcl}
 2x_1 & +3x_2 & +x_3 & \leq & 5 \\
 4x_1 & +x_2 & +2x_3 & \leq & 11 \\
 3x_1 & +4x_2 & +2x_3 & \leq & 8
 \end{array}$$

	Z	$x_1$	$x_2$	$x_3$	$s_1$	$s_2$	$s_3$	$b$
Z	1	0	3	0	1	0	1	?
$s_2$	0	0	-5	0	-2	1	0	?
$x_3$	0	0	-1	1	-3	0	2	?
$x_1$	0	1	2	0	+2	0	-1	?

**Question:** (Tableau is optimal for LP with given constraints.)

- A. Then one of the four questionmarks is 2
- B. Then one of the four questionmarks is 3
- C. Then one of the four questionmarks is 4
- D. Then one of the four questionmarks is 5

## Clicker #B.2

	Z	$x_1$	$x_2$	$s_1$	$s_2$	$s_3$	$b$
Z	1	-3	??	0	0	0	0
$s_1$	0	1	0	1	0	0	4
$s_2$	0	0	??	0	1	0	12
$s_3$	0	3	?!?	0	0	1	18

	Z	$x_1$	$x_2$	$s_1$	$s_2$	$s_3$	$b$
Z	1	0	0	0	$1\frac{1}{2}$	1	36
$s_1$	0	0	0	1	$\frac{1}{3}$	$-\frac{1}{3}$	2
$x_2$	0	0	??	0	$\frac{1}{2}$	0	6
$x_1$	0	1	??	0	$-\frac{1}{3}$	$\frac{1}{3}$	2

**Question:** (Starting tableau and final tableau)

- A. Then ?!?
- B. Then ?!?
- C. Then ?!?
- D. Then ?!?

## Clicker #C.1

Consider LP with objective

$$\text{minimize } 3x_1 - 5x_2 + x_3 + x_4$$

subject to a system of constraints.

The point  $(1, 5, 9, 6)$  is feasible for the primal LP.

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**Question:** Which of the following statements could possibly be true?

- A. The dual LP is infeasible
- B. The dual LP is unbounded
- C. The optimal objective value of the dual LP is  $-6$
- D. The optimal objective value of the dual LP is at least  $-5$

## Clicker #C.2

Consider LP with objective

$$\text{minimize } 2x_1 + x_2 - x_3 + x_4$$

subject to a system of constraints.

The point  $(1, 3, 5, 2)$  is feasible for both the primal and the dual LP.

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**Question:** Which objective is possible for the dual LP?

- A. maximize  $y_1 + y_2 + y_3 + y_4$
- B. maximize  $2y_1 + y_2 - y_3 - y_4$
- C. minimize  $2y_1 + y_2 - y_3 + y_4$
- D. maximize  $2y_1 + 2y_2 - y_3 + y_4$



# Clicker #C.3

$$2x_1 + 3x_2 + x_3 \leq 3$$

$$4x_1 + x_2 + 2x_3 \leq 1$$

$$3x_1 + 4x_2 + 2x_3 \leq 8$$

	Z	$x_1$	$x_2$	$x_3$	$s_1$	$s_2$	$s_3$	$b$
Z	1	0	3	0	1	0	2	?
$s_2$	0	0	-5	0	?	1	0	?
$x_3$	0	0	-1	1	?	0	2	?
$x_1$	0	1	2	0	?	0	1	?

**Question:** (Tableau is optimal for LP with given constraints.)

- A. Then  $2x_1 + 3x_2 + x_3 < 3$  is possible
- B. Then  $4x_1 + x_2 + 2x_3 < 1$  is possible
- C. Then  $3x_1 + 4x_2 + 2x_3 < 8$  is possible
- D. None of the above

# Clicker #C.4

$$\begin{array}{rclcl} 2x_1 & +3x_2 & +x_3 & \leq & 7 \\ x_1 & +x_2 & +2x_3 & \leq & 13 \\ 3x_1 & +4x_2 & +2x_3 & \leq & ? \end{array}$$

	Z	$x_1$	$x_2$	$x_3$	$s_1$	$s_2$	$s_3$	$b$
Z	1	0	3	0	1	0	2	?
$s_2$	0	0	-5	0	-2	1	0	?
$x_3$	?	?	?	?	?	?	?	?
$x_1$	?	?	8	?	?	?	?	2

**Question:** In this optimal tableau,

- A. variable  $x_3$  has value 1
- B. variable  $x_3$  has value 2
- C. variable  $x_3$  has value 3
- D. variable  $x_3$  has value 4

# Clicker #C.5

$$x_1 + 3x_2 + 2x_3 \leq 13$$

$$x_1 + x_2 + x_3 \leq 11$$

$$x_1 + 2x_2 + 3x_3 \leq 18$$

	Z	$x_1$	$x_2$	$x_3$	$s_1$	$s_2$	$s_3$	$b$
Z	1	0	2	0	3	0	2	?
$s_2$	0	0	-5	0	?	1	0	?
$x_3$	0	0	?	1	?	0	2	?
$x_1$	0	1	2	0	?	0	1	?

**Question:** (Tableau is optimal for LP with given constraints.)

- A. Then  $x_1 + x_3 = 8$
- B. Then  $x_1 + x_3 = 9$
- C. Then  $x_1 + x_3 = 10$
- D. None of the above

# Clicker #C.6

$$\begin{array}{rclcl} 2x_1 & +3x_2 & +x_3 & \leq & 6 \\ 4x_1 & +2x_2 & +2x_3 & \leq & 12 \\ x_1 & +4x_2 & +3x_3 & \leq & 7 \end{array}$$

	Z	$x_1$	$x_2$	$x_3$	$s_1$	$s_2$	$s_3$	$b$
Z	1	0	3	0	1	0	?	17
$s_2$	0	0	8	0	-2	1	0	?
$x_3$	0	0	?	1	-3	0	2	2
$x_1$	0	1	?	0	+2	0	1	2

**Question:** (Final tableau for LP.)

- A. Then  $y_3 = 1$  is possible
- B. Then  $y_3 = 2$  is possible
- C. Then  $y_3 = 3$  is possible
- D. None of the above

## Clicker #D.1

Consider the transportation problem

8	9	21	6		9
22	1	13	9		3
3	4	5	1		6
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5	4	5	$d_4$		

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**Question:** If total supply equals total demand,

- A. then  $d_4 = 2$
- B. then  $d_4 = 3$
- C. then  $d_4 = 4$
- D. none of the above

## Clicker #D.2

Here is a basic feasible solution for a transportation problem:

9	?	?	?		9
?	3	2	?		5
?	?	?	4		4
<hr/>					
9	3	2	4		

$X$  = number of questionmarks that are in the basis.

$Y$  = number of questionmarks that are non-zero.

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Question:

- A. Then  $X = 1$  and  $Y = 5$
- B. Then  $X = 2$  and  $Y = 0$
- C. Then  $X = 3$  and  $Y = 8$
- D. Then  $X = 3$  and  $Y = 6$

## Clicker #D.3

Here is a basic feasible solution for a transportation problem:

7	1	?	?		8
?	2	3	?		5
?	?	?	3		4
<hr/>					
7	3	3	4		

$X$  = number of questionmarks that are in the basis.

$Y$  = number of questionmarks that are non-zero.

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**Question:**

- A. Then  $X = 1$  and  $Y = 1$
- B. Then  $X = 1$  and  $Y = 2$
- C. Then  $X = 2$  and  $Y = 1$
- D. None of the above.

## Clicker #D.4

While we are solving an instance of the transportation problem, we encounter a chain reaction that involves exactly  $R$  entries.

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**Question:** Which of the following options is a possible value for  $R$ ?

- A.  $R = 2$
- B.  $R = 7$
- C.  $R = 12$
- D.  $R = 17$



## Clicker #D.5

Consider the transportation problem

1	4	5		7
9	9	1		1
9	1	2		2
<hr/>				
3	3	4		

North-West corner rule generates starting solution of cost NW.  
Minimum Cost rule generates starting solution of cost MC.

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Question:

- A.  $NW - MC = -1$
- B.  $NW - MC = 0$
- C.  $NW - MC = 1$
- D.  $NW - MC = 2$

## Clicker #D.6

We use the North-West corner rule to compute a starting solution for an  $m \times m$  assignment problem.

Let  $X$  denote the number of 0-entries in this solution.

Let  $Y$  denote the number of 1-entries in this solution.

Let  $Z$  denote the number of entries  $\geq 2$  in this solution.

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Question:

- A. Then  $X = m$  and  $Y = m$  and  $Z > 0$ .
- B. Then  $X = m - 1$  and  $Y = m$  and  $Z = 0$ .
- C. Then  $X = m$  and  $Y = m - 1$  and  $Z = 0$ .
- D. Then  $X = m - 1$  and  $Y = m - 1$  and  $Z \neq 0$ .