

**EINDHOVEN UNIVERSITY OF TECHNOLOGY**  
**Department of Mathematics and Computer Science**

*Examination Real-time Architectures (2IN25)*  
*on Friday, June 13<sup>th</sup> 2008, 14.00h-17.00h.*

First read the entire examination. There are 6 exercises in total. Grades are included between parentheses at all parts and sum up to 9 points. Good luck!

1. A typical recursive equation to determine the worst-case response time of a task  $\tau_i$  under fixed-priority pre-emptive scheduling (FPPS) is given by

$$x = C_i + \sum_{j \in hp(i)} \left\lceil \frac{x}{T_j} \right\rceil C_j,$$

where  $hp(i)$  denotes the set of tasks with a *higher priority* than  $\tau_i$  and tasks have distinct priorities.

- (a) (0.5) Give at least two additional assumptions that need to hold to use this equation.  
**Answer** Examples: (i) tasks are independent, (ii) deadlines are at most equal to periods, i.e.  $D_i \leq T_i$ , and (iii) tasks do not suspend themselves. Note that tasks need not be strictly periodic, e.g. the equation is also valid for elastic and sporadic tasks.

An RTOS (Real-Time Operating System) typically only provides a limited number of priority levels. Hence, multiple tasks may have to *share* a priority level. Let  $ep(i)$  denote the set of tasks with priority equal to that of  $\tau_i$ .

- (b) (0.5) Extend the recursive equation given above to account for multiple tasks sharing a priority level. Motivate your answer.  
**Answer** The worst-case response time is assumed when a task  $\tau_i$  is simultaneously released with all tasks in  $hp(i) \cup ep(i)$ , and is the last task from  $ep(i) \cup \{\tau_i\}$  that is allowed to execute. Note that it is assumed that  $i \notin ep(i)$ .

The easiest approach to analyse the system is to treat all tasks in  $ep(i)$  as higher priority tasks, i.e.

$$x = C_i + \sum_{j \in hp(i) \cup ep(i)} \left\lceil \frac{x}{T_j} \right\rceil C_j.$$

This is pessimistic, however, because *at most one job* of every task  $\tau_j \in ep(i)$  can delay the execution of  $\tau_i$ , and we therefore get

$$x = C_i + \sum_{j \in ep(i)} C_j + \sum_{j \in hp(i)} \left\lceil \frac{x}{T_j} \right\rceil C_j.$$

2. Consider (fixed-priority) servers.

- (a) (0.5) Describe how a server compares to background scheduling.  
**Answer** See book.

- (b) (0.5) Under which conditions does a deferrable server behave as a periodic task without self-suspension?

**Answer** When there is always work pending for the deferrable server if its capacity is larger than zero.

3. (2.0) Let tasks  $\tau_1$  and  $\tau_2$  both use resources  $r_1$  and  $r_2$ . Task  $\tau_1$  first locks  $r_1$  and subsequently  $r_2$ , and  $\tau_2$  first locks  $r_2$  and subsequently  $r_1$ , which may give rise to a deadlock without a resource access protocol; see Figure 1. Discuss what happens when a resource

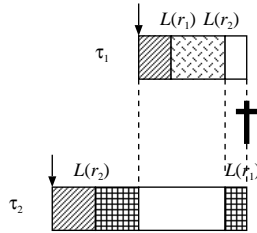


Figure 1: A deadlock situation.

access protocol is used and illustrate the behavior by means of appropriate drawings for PIP, HLP, PCP, and SRP.

**Answer** This exercise has been taken from RTA.Exercises-4 (2007/2008).

4. (1.0) Give an example of a task set that is schedulable with fixed-priority non-pre-emptive scheduling (FPNS) but is *not* schedulable with fixed-priority pre-emptive scheduling (FPPS).

**Answer** Compared to FPPS, FPNS can *decrease* the worst-case response time of lower priority tasks. Hence, we could aim at creating a task-set where

- a lower priority task is not schedulable under FPPS;
- that lower priority task is schedulable under FPNS;
- all other tasks are also schedulable under FPNS.

Table 1 provides an example of such a task-set (assuming arbitrary phasing), where  $\tau_1$  has highest and  $\tau_3$  has lowest priority.

	$T$	$C$
$\tau_1$	9	2
$\tau_2$	11	2
$\tau_3$	12	6

Table 1: A task-set schedulable under FPNS but not under FPPS.

Alternative approaches: assume a specific phasing or assume resource sharing between a highest and lowest priority task *without* a resource access protocol (and a middle priority task that preempts the lowest priority task during resource access under FPPS).

5. (2.0) Consider the system configuration shown in Figure 2, with characteristics as given in Table 2. The input streams are (strictly) periodic and have arbitrary phasing. The tasks are scheduled by means of FPPS, where  $\tau_1$  has highest priority and task  $\tau_3$  has lowest priority. Determine the worst-case end-to-end delay of an event of input stream  $I_2$ . (*Hint:*

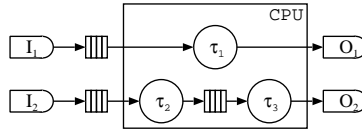


Figure 2: System configuration.

	$T$		$C$
$I_1$	80	$\tau_1$	21
$I_2$	50	$\tau_2$	20
		$\tau_3$	10

Table 2: Characteristics of input streams and tasks.

(determine a critical instant and use a timeline.)

**Answer** A worst-case situation is characterized by a simultaneous arrival of both events  $I_1$  and  $I_2$ . The behavior of the system under worst-case conditions is shown in Figure 3.

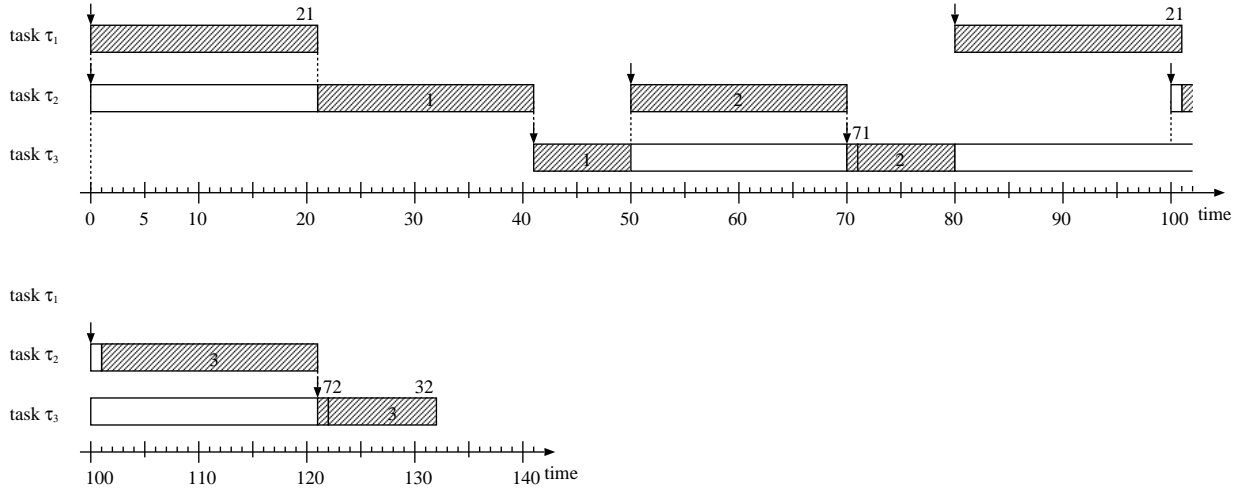


Figure 3: Timeline of tasks, where the numbers at the top-right corner of the boxes represent end-to-end response times of  $I_1$  and  $I_2$ .

The end-to-end response times of  $I_{2,k}$  are given in Table 3, where  $R_{I_{2,k}} = R_{2,k} + R_{3,k}$ . The worst-case end-to-end response time  $WR_{I_2} = 72$ . Note that  $WR_{I_2} < \max_k R_{2,k} + \max_k R_{3,k} = 41 + 52 = 93$ .

Task  $\tau_3$  is triggered by  $\tau_2$ , and the *activation* of  $\tau_3$  therefore coincides with the *completion* of  $\tau_2$ . When the temporal offset between the tasks is not taken into account, the analysis becomes very pessimistic. As an example, assuming an activation of task  $\tau_3$  at time  $t = 0$  rather than  $t = 41$  would yield a response time  $R_{3,1} = 71$  rather than 30, and an end-to-end delay of 112.

6. The lecture of Dr. Alina Weffers-Albu concerned *Behavioral Analysis of Real-Time Systems with Interdependent Tasks*.

(a) (1.0) Explain which real-time problems were addressed.

	$k = 1$	2	3
$R_{2,k}$	41	20	21
$R_{3,k}$	30	52	11
$R_{I_2,k}$	71	72	32

Table 3: Response times of tasks  $\tau_2$  and  $\tau_3$  and end-to-end response times of the input stream  $I_2$ .

- (b) (0.5) Explain how these problems have been solved.
- (c) (0.5) Explain why these approaches were taken.

**Answers** See slides of the lecture.