

**EINDHOVEN UNIVERSITY OF TECHNOLOGY**  
**Department of Mathematics and Computer Science**

*Examination Real-time Architectures (2XN26)*  
*on Tuesday, November 1<sup>st</sup> 2011, 14.00h-15.30h.*

First read the entire examination. There are 5 exercises in total. Grades are included between parentheses at all parts and sum up to 10 points. Good luck!

1. This exercise concerns general aspects of real-time systems.
  - (a) (0.5) Timing requirements can be classified as either *functional* requirements or as *quality* requirements. When should which classification be used?
  - (b) (0.5) Is “real time” the same as “fast”? Motivate your answer.
  - (c) (0.5) The so-called 4+1 view model of Kruchten consists of a *logical view*, *development view*, *process view*, *deployment view* and *scenarios*. Which view is the *least* relevant for real-time systems and why?
  - (d) (0.5) Give at least three characteristics of embedded systems.

**Answer:** See RTS.A1-Introduction.

2. A control system monitors its environment by means of sensors and responds via actuators. Monitoring can be performed by either *time*-triggered tasks or *event*-triggered tasks.
  - (a) (0.5) Explain the difference between *time*- and *event*-triggered tasks in your own words.
  - (b) Let the deadline for a response of the control system for a given event be given by  $D^{System}$ . Assume computation and actuation is done by a (single) time-triggered task  $\tau$ .
    - i. (0.5) Draw a worst-case situation for the arrival of the task  $\tau$ .
    - ii. (0.5) Give a *schedulability condition* for task  $\tau$ , based on  $D^{System}$ , and the period  $T^\tau$  and deadline  $D^\tau$  of  $\tau$ .

**Answer:** See RTS.D0-Water-Vessel.

3. To implement periodic tasks,  $\mu\text{C}/\text{OS-II}$  provides
  - *relative one-shot* timers, i.e. `void OSTimeDly(INT16U ticks)`, where `ticks` are the number of clock ticks; and
  - primitives to set and get time, i.e. `void OSTimeSet(INT32U ticks)` and `INT32U OSTimeGet(void)`.
  - (a) (0.5) Explain the notions of *relative* timer and *one-shot* timer in your own words.
  - (b) (1.0) Is the functionality provided appropriate to implement periodic tasks?  
*Hint: discuss jitter and drift.*

**Answer:** See RTS.Exercises-3.

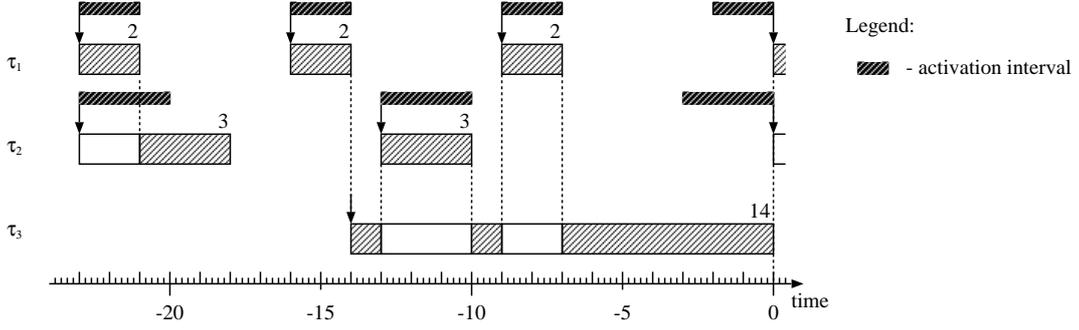


Figure 1: Timeline with an optimal instant for task  $\tau_3$ .

4. Consider three tasks that are scheduled by means of fixed-priority pre-emptive scheduling (FPPS), where  $\tau_1$  has highest and  $\tau_3$  has lowest priority, with arbitrary phasing and characteristics as given in the following table.

	$T$	$WD$	$BD$	$AJ$	$WC$	$BC$
$\tau_1$	7	5	2	2	2	2
$\tau_2$	10	7	2	3	3	3
$\tau_3$	31	25	11	5	9	9

- (a) Consider the following recursive equation.

$$x = B_i + WC_i + \sum_{1 \leq j < i} \left\lceil \frac{x + AJ_j}{WT_j} \right\rceil WC_j. \quad (1)$$

- i. (0.5) Determine the smallest positive solution of (1) for task  $\tau_3$ .

**Answer:** Note that the *lowest* priority task is *never* blocked. Hence,  $B_3 = 0$  irrespective of potential resource sharing. Using an iterative procedure, we find  $WR_3 = 26$ .

- ii. (0.5) Is this value the worst-case response time  $WR_3$  of  $\tau_3$ ?

**Answer:** Yes, because  $WR_3 + AJ_3 = 31 \leq T_3 = 31$ , hence a job of  $\tau_3$  never experiences interference of a previous job of  $\tau_3$ .

- (b) Determine the best-case response time of task  $\tau_3$

- i. (0.5) by drawing a time line with an optimal instant for  $\tau_3$ .

**Answer:** See Figure 1. Note that  $BR_3 = 14$ .

- ii. (0.5) by means of the following recursive equation.

$$x = BC_i + \sum_{1 \leq j < i} \left( \left\lceil \frac{x - AJ_j}{BT_j} \right\rceil - 1 \right)^+ BC_j \quad (2)$$

**Answer:** Using  $WR_3 = 26$  as initial value for the iterative procedure to determine the best-case response time  $BR_3$ , we find  $BR_3 = 14$ .

- (c) (0.5) Is task  $\tau_3$  schedulable?

**Answer:** No, because  $WR_3 = 26 > WD_3 = 25$ .

5. This exercise concerns resource access protocols (RAPs).

- (a) (1.0) Transitive priority adjustment may occur when applying the Priority Inheritance Protocol (PIP). Describe at least three conditions that need to hold for transitive priority adjustment to occur.

**Answer:** We essentially need to describe conditions that may give rise to transitive blocking: (1) at least three tasks, e.g.  $\tau_h$ ,  $\tau_m$ , and  $\tau_l$ , with distinct priorities, where  $\tau_h$  has highest and  $\tau_l$  has lowest priority; (2) at least two mutual exclusive resources, e.g.  $R_1$  and  $R_2$ ; (3)  $\tau_h$  uses a resource  $R_1$ ,  $\tau_l$  uses  $R_2$ , and  $\tau_m$  uses  $R_1$  and  $R_2$  in a nested fashion, i.e. it first locks  $R_1$  and then locks  $R_2$  before releasing  $R_1$ .

- (b) (0.5) The Priority Ceiling Protocol (PCP) and the Stack Resource Policy (SRP) are both based on resource ceilings. They differ with respect to the *moment* blocking occurs. Describe the difference in your own words.

**Answer:** Blocking occurs upon an attempt to

- *lock* a resource under PCP, i.e. *resource access*;
- *start* execution (of a job) under SRP, i.e. *on preemption*.

See RTS.B4-Policies-3-RAP.

- (c) (0.5) SRP differs from PIP, HLP, and PCP in an essential aspect when it concerns priorities. Explain that difference in your own words.

**Answer:** The priority of a task is not changed under SRP. Instead, the priority in combination with the *system ceiling* determines which tasks may preempt under SRP. As an alternative, one may observe that SRP can also be used for *dynamic* priorities, whereas the other policies only apply for *fixed* priorities.

- (d) (0.5) PIP is stated to be a *transparent* RAP. Explain transparency in your own words.

**Answer:** See book Buttazzo p. 230.